

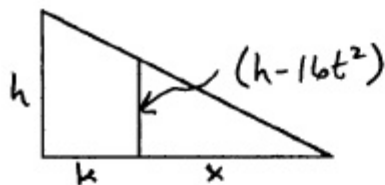
1.  $y = 2x - 3$  &  $y = 2x + 3$  From the first equation, we get  $\frac{dy}{dx} = \frac{-2}{(x-1)^2}$ . The slope of the 2<sup>nd</sup> equation is 2.

Therefore,  $\frac{(x-1)^2}{2} = 2$  (slope of  $\perp$ ). This gives  $x = -1$  or 3, which give the required equations.

2.  $\boxed{-3}$   $P(0) = 1$  implies  $d = 1$  and  $a = c = 0$  due to symmetry.  $P(q) = q^4 + bq^2 + 1 = -3$  and  $P'(q) = 4q^3 + 2bq = 0$ . Solving this 2<sup>nd</sup> equation gives  $q = 0$  or  $b = -2q^2$ . Plugging into the 1<sup>st</sup> equation gives  $b = -4$  and  $a + b + c + d = -3$ .

3.  $\boxed{2 \text{ weeks}}$  Let  $x =$  the number of weeks to wait. Income =  $I = (160 + 40x)(2 - .2x - .05x) = 10(32 + 4x - x^2)$ .  $I' = 10(4 - 2x) = 0$  at  $x = 2$ . The 2<sup>nd</sup> derivative is negative, meaning that  $x = 2$  is a max.

4.  $\boxed{-kb}$   $\frac{x}{b - 16t^2} = \frac{k}{16t^2} \Rightarrow x = \frac{kb - 16kt^2}{16t^2}$ . And  $\frac{dx}{dt} = v(t) = \frac{16t^2(-32kt) - (kb - 16kt^2)(32t)}{(16t^2)^2}$  and  $v(\frac{1}{2}) = -kb$ .



5.  $\boxed{25,000}$   $\frac{dy}{dt} = 1000e^{-t/20}(1 - \frac{t}{20})$ . At  $t = 0$ ,  $y = 25000$  and at  $t = 20$ ,  $y = 32358$  and at  $t = 100$ ,  $y = 25674$ . therefore the minimum is at  $y = 25,000$ .

6.  $\boxed{\frac{50}{3}}$  Splitting the region into a rectangle and another region gives Area =  $6 + \int_0^4 \frac{5x^2 + 16}{16} dx = 6 + \frac{32}{3} = \frac{50}{3}$ .

7.  $\boxed{-\sqrt{2} \sin \theta}$  Note that  $\sqrt{1 - \cos 2\theta} = \sqrt{2 \sin^2 \theta} = \sqrt{2} \sin \theta$ . So, now  $r = \frac{\sqrt{2} \sin \theta}{\tan \theta} = \sqrt{2} \cos \theta \Rightarrow \frac{dr}{d\theta} = -\sqrt{2} \sin \theta$ .

8.  $\boxed{e^{-x} + \sin x}$  Using patterns we get,  $(-1)^{100} e^{-x} + \sin x = e^{-x} + \sin x$ .

9.  $\boxed{k = 5}$   $R_x = \pi \int_0^k (kx - x^2) dx = \frac{\pi k^5}{30}$  and  $R_y = 2\pi \int_0^k x(kx - x^2) dx = \frac{\pi k^4}{6}$ .  $R_x = R_y$ , at  $k = 5$ .

10.  $\boxed{(0, 0)}$   $f'(x) = \frac{4}{3}x^{\frac{1}{3}} + \frac{4}{3}x^{-\frac{2}{3}}$ . As  $x \rightarrow 0$ ,  $f'(x) \rightarrow \infty$ . Therefore, there is a vertical tangent at  $(0, 0)$ .

11.  $4x - 3y = 43$   $x = 7$  implies  $y = -5$  or  $y = 1$ . Also,  $2x + 2yy' - 6 + 4y' = 0 \Rightarrow y' = \frac{3-x}{y+2}$  and at  $(7, -5)$  we get the answer.

12.  $90 \text{ in/sec}$   $a = \frac{dv}{dt} = 6t \Rightarrow dv = 6t dt \Rightarrow v = 3t^2 + c = \frac{ds}{dt} \Rightarrow ds = (3t^2 + c)dt \Rightarrow s = t^3 + ct + k$ . So,  $s(1) = 10 = 1 + c + k$  and  $s(2) = 80 = 8 + 2c + k$ . And,  $c = 63$  &  $k = -54$ . This yields  $v = 3t^2 + 63$  and  $v(3) = 90$ .

13.  $-1 \leq x < 5$  Using the Ratio Test, we get  $R = \lim_{n \rightarrow \infty} \left| \frac{(x-2)^{n+1}}{(n+1)3^{n+1}} \cdot \frac{n3^n}{(x-2)^n} \right| = \left| \frac{x-2}{3} \right|$ . This converges if

$\left| \frac{x-2}{3} \right| < 1$  or  $-1 < x < 5$ . Checking endpoints: At  $x = 5$ , it diverges (harmonic series) and at  $x = -1$ , it converges (alternating harmonic series).

14.  $\boxed{2}$   $W = \int_1^4 x^{-1/2} dx = 2 \text{ ft-lbs.}$

15.  $x^x(1 + \ln x)$  Taking the natural log of both sides gives  $\ln y = \ln(x^x) \Rightarrow x \ln x$ . Differentiating both sides gives  $\frac{1}{y} y' = x \cdot \frac{1}{x} + \ln x = 1 + \ln x$ . Multiplying by  $y$  and substituting back in for  $y$  gives the answer.